

Internal Resistance MS

M1. (a) (i) (use of $V = IR$)

$$R_{\text{total}} = 1 \text{ (ohm)} \checkmark$$

$$V = 1 \times 1 = 1.0 \text{ V} \checkmark$$

2

(ii) (use of $V = IR$)

$$R = 9.0/1.0 = 9.0 \Omega \checkmark$$

$$r = 9.0 - 1.0 - 6.0 = 2.0 \Omega \checkmark$$

or use of ($E = I(R + r)$)

$$9.0 = 1(7 + r) \checkmark$$

$$r = 9.0 - 7.0 = 2.0 \Omega \checkmark$$

2

(iii) (use of $W = VIt$)

$$W = 9.0 \times 1.0 \times 5 \times 60 \checkmark$$

$$W = 2700 \text{ J} \checkmark$$

2

(iv) energy dissipated in internal resistance = $I^2 \times 2.0 \times 5 \times 60 = 600 \text{ (J)}$ \checkmark

$$\text{percentage} = 100 \times 600/2700 = 22\% \checkmark \text{ CE from part aii}$$

2

(b) internal resistance limits current \checkmark

hence can provide higher current \checkmark

or energy wasted in internal resistance/battery \checkmark

less energy wasted (with lower internal resistance) \checkmark

or charges quicker \checkmark

as current higher or less energy wasted \checkmark

or (lower internal resistance) means higher terminal pd/voltage \checkmark

as less pd across internal resistance or mention of lost volts \checkmark

2

[10]

M2. (a) (i) energy changed to electrical energy per unit charge/coulomb passing through
[or electrical energy produced per coulomb or unit charge]
[or pd when no current passes through/or open circuit] **(1)**

(ii) $I = \frac{6}{2.4} = 2.5 \text{ A}$ **(1)**

(iii) (use of $\epsilon = I(R + r)$ gives) $\epsilon = V + Ir$ and $8 = 6 + Ir$ **(1)**

substitution gives $8 - 6 = 2.5r$ **(1)** (and $r = 0.8 \Omega$)

4

(b) (i) (use of $P = I^2R$ gives) $P_R = 2.5^2 \times 2.4 = 15 \text{ W}$

[or $P = VI$ gives $P = 6 \times 2.5 = 15 \text{ W}$] **(1)**

(allow C.E. for value of I from (a))

(ii) $P_T = 15 + (2.5^2 \times 0.8)$ **(1)**

$= 20 \text{ (W)}$ **(1)**

(allow C.E. for values of P_R and I)

(iii) $E = 5 \times 2 \times 60 = 600 \text{ J}$ **(1)**

(allow C.E. for value of P from (i) and P_T from (ii))

4

[8]

M3. (i) ($V = IR$ gives) $12 = (30 + 30 + 2)I$ (1)

$$I = \left(\frac{12}{62} \right) = 0.19 \text{ A (1)} \quad (0.194 \text{ A})$$

(ii) $V_{PQ} = 12 - (0.19 \times 2)$ (1)
 $= 11.6 \text{ V (1)}$

(allow C.E. for incorrect I in (i))

[or $V_{PQ} = 0.19 \times 60 = 11.6 \text{ V}$ ($I = 0.194 \text{ A}$ gives 11.6 V)

[or $V_{PQ} = 12 \times \frac{60}{62} = 11.6 \text{ V}$

(iii) ($P_A = I^2 R$ gives) $P_A = (0.19)^2 \times 30 = 1.08$ (1) W (1)

[or $P_A = \frac{V^2}{R}$]

(allow C.E. for incorrect I in (i) or incorrect V in (ii))

(iv) ($E = P_A t$ gives) $E = 1.08 \times 20$ (1)

$= 21.6 \text{ J (1)}$

(allow C.E. for incorrect P_A in (iii))

[8]

M4. (a) (i) work (done)/energy (supplied) per unit charge (by battery) (1)

(or pd across terminals when no current passing through cell or open circuit)

1

(ii) when switch is closed a **current flows** (through the battery) (1)

hence a pd/lost volts develops across the internal resistance (1)

2

(b) (use of $\epsilon = V + Ir$)

$I = 5.8/10 = 0.58 \text{ (A) (1)}$

$6.0 = 5.8 + 0.58r$ (1)

$r = 0.2/0.58 = 0.34 \text{ (}\Omega\text{) (1)}$

3

- (c) need large current/power to start the car **(1)** (or current too low)

internal resistance limits the current/wastes power(or energy)/reduces terminal pd/increases lost volts **(1)**

2

[8]

- M5.** (a) (use of $E = V + Ir$)

$$12 = V + 420 \times 0.0095 \text{ (1)}$$

$$V = 8.0(1)\text{V (1)}$$

2

- (b) $\rho = RA/I = 1.6 \times 10^{-3} \times 7.9 \times 10^{-5}/0.75 \text{ (1)}$

$$R = 1.7 \times 10^{-7} \text{ (1) } \Omega\text{m (1)}$$

3

[5]

- M6.** (a) (i) work done (by the battery) per unit charge **(1)**
or (electrical) energy per unit charge
or pd/voltage when open circuit/no current

- (ii) the resistance of the materials within the battery **(1)**
or hindrance to flow of charge **in** battery
or loss of pd/voltage per unit current

2

- (b) (i) (use of $E = V + Ir$)

$$12 = V + 800 \times 0.005 \text{ (1) (working/equation needs to be shown)}$$

$$V = 12 - 4 = 8.0\text{V (1)}$$

- (ii) (use of $P = I^2 r$)

$$P = 800^2 \times 0.005 \text{ (1) (working/equation needs to be shown)}$$

$$P = 3200 \text{ (1) W (1) or } \text{J s}^{-1}$$

5

(c) car will probably **not** start (1)

battery will not be able to provide enough current (1)

or less current

or lower terminal pd/voltage

2

[9]

M7. (a) mention of pd across internal resistance **or** energy loss
in internal resistance **or** $\text{emf} > V$ ✓

pd across internal resistance/lost volts increases with
current **or** correct use of equation to demonstrate ✓

2

(b) (i) y – intercept 1.52 V (± 0.01 V) ✓

1

(ii) identifies gradient as r **or** use of equation ✓

substitution to find gradient **or** substitution in equation ✓

$$r = 0.45 \pm 0.02 \Omega \checkmark$$

3

(c) (i) same intercept ✓

double gradient (must go through 1.25, 0.40 ± 1.5 squares) ✓

2

(ii) same intercept horizontal line ✓

1

(d) (i) (use of $Q = It$)

$$Q = 0.89 \times 15 = 13 \checkmark \text{ C } \checkmark$$

2

(ii) use of $P = I^2 r$ ✓

$$P = 0.89^2 \times 0.45$$

$$P = 0.36 \text{ W } \checkmark$$

2

[13]

M8. (a) **battery** has internal resistance (1)

current passes through (this resistance) (1)

work done/voltage lost, which reduces the value of the emf (1)

3

QWC 1

- (b) (i) circuit diagram to show:
two **cells** in series **(1)**
two resistors, each labelled r **(1)**
- (ii) (use of $P = IV$ gives) $1.6 = 2.5 I$ **(1)** ($I = 0.64$ (A))
(use of $\epsilon = V + Ir$ gives) $3.0 = 2.5 + 0.64 \times 2r$ **(1)** **(1)**
 $0.5 = 1.28r$ and $r = 0.39 \Omega$ **(1)**
[or $R_{\text{bulb}} = 2.5^2/1.6 = 3.9$ (Ω) and $2.5 = 3.9 \times I$ gives $I = 0.64$ (A)
'lost volts' = $(3 - 2.5) = 0.5$ (V) i.e. 0.25 (V) per cell
 $0.25 = 0.64r$ and $r = 0.39 \Omega$]

5

- (c) $\epsilon = V + Ir$ gives $V = -Ir + \epsilon$ (equation of straight line) **(1)**
intercept on y -axis gives ϵ **(1)**
gradient gives $(-r)$ **(1)**

3

[11]

M9. (a) $V = -Ir + \epsilon$ **(1)**

1

- (b) straight line (within 1st quadrant) **(1)**
negative gradient **(1)**

2

- (c) ϵ : intercept on voltage axis **(1)**
 r : gradient **(1)**

2

[5]

M10. (a) (i) 6.0 (Ω) **(1)**

1

(ii) 4.5 (V) **(1)**

1

- (iii) (use of $I = V/R$)

$I = 4.5/6.0 = 0.75$ (A) **(1)**

current through cell A = $0.75/2 = 0.375$ (A) **(1)**

2

(iv) charge = $0.375 \times 300 = 112$ **(1)** C **(1)**

2

- (b) cells C and D will go flat first or A and B last longer **(1)**

current/charge passing through cells C and D (per second) is double/more than that passing through A or B **(1)**

energy given to charge passing through cells **per second** is double or more than in cells C and D **(1)** or in terms of power

3

[9]

- M11.** (a) (i) electrical energy produced (in the battery) per unit charge **(1)**

[or potential/voltage across terminals when there is no current]

- (ii) there is a current (through the battery) **(1)**

voltage 'lost' across the internal resistance **(1)**

Max 2

- (b) (i) $\epsilon = V + Ir$ **(1)**

- (ii) labelled scales **(1)**

correct plotting **(1)**

best straight line **(1)**

ϵ : intercept on y axis **(1)** = 9.2 (\pm 0.1) V **(1)**

$$r: (-) \text{ gradient} = \frac{9.2}{0.65} = 14.2 \Omega \text{ (1) (range 14.0 to 14.3)}$$

8

[10]